



I E G U L D Ī J U M S T A V Ā N Ā K O T N Ē

6. atskaite par posmu no 13.10.2021. līdz 13.05.2021.

Par Latvijas Universitātes projekta “Uz čukstošās galerijas modas mikrorezonatora bāzes veidota optisko frekvenču ķemmes ģenerators izstrāde un tā pielietojumi telekomunikācijās” Nr. 1.1.1.1/18/A/155 norisi

Projekta vispārējais mērķis: Veikt pētniecību, kas veicina Latvijas viedās specializācijas stratēģijas mērķu sasniegšanu, cilvēkkapitāla attīstību zinātnē un tehnoloģijās un jaunu zināšanu radīšanu, lai uzlabotu konkurētspēju tautsaimniecībā.

Projekta mērķis ir: iegūt jaunas zināšanas par čukstošo galeriju modu rezonatoru optiskajām frekvenču ķemmēm (WCOMBs) un izstrādāt, konstruēt un testēt ķemmes ģenerators prototipu telekomunikāciju pielietojumiem.

Prezentēja: Jānis Alnis, MS Teams, LU ASI 2022. g. 3. maijā.

Whispering gallery microresonator basics

- Use total internal reflection
- Do not need mirror coatings
- Work in broad wavelength range
- Can be made in house
- Simple enough for Latvia
- Sensors, nonlinear optics

Optical quality factor Q

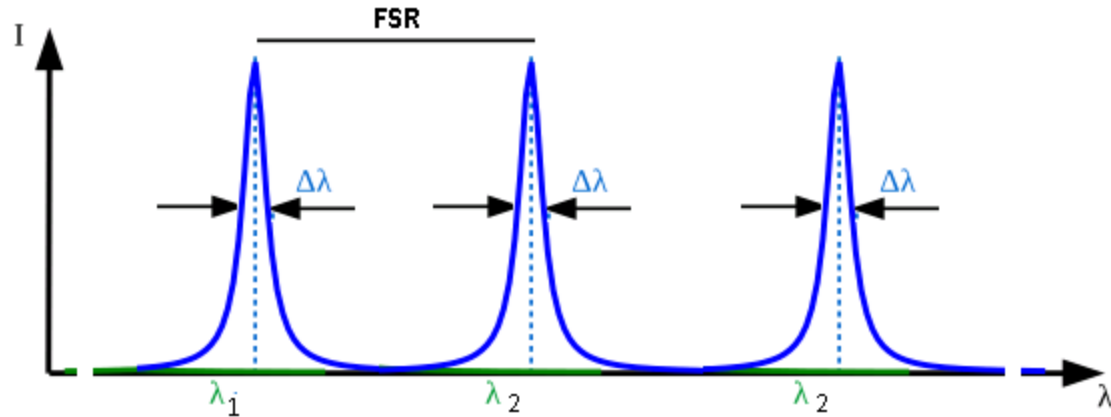
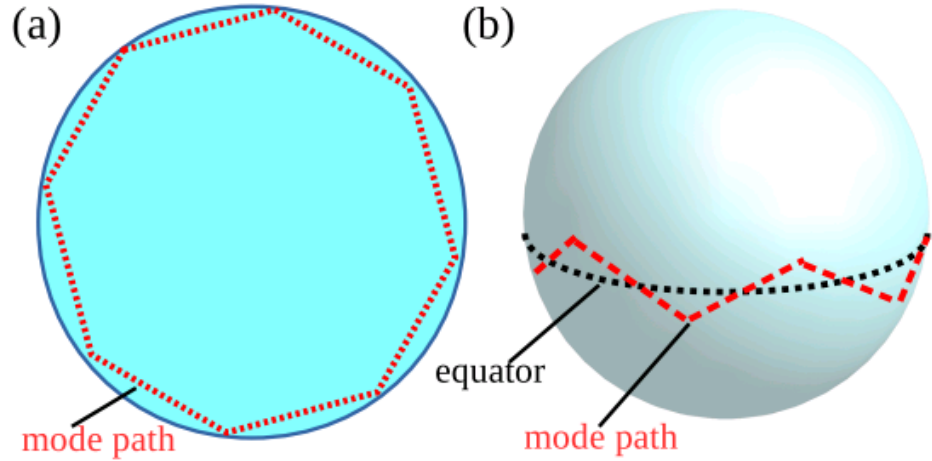
$Q = \omega \tau$,
where τ is the photon lifetime

$Q = \nu / \Delta \nu = \lambda / \Delta \lambda$,
where ν is the optical frequency
and $\Delta \nu$ is the linewidth

$Q = 2\pi L / \lambda$
where L is the photon path length.

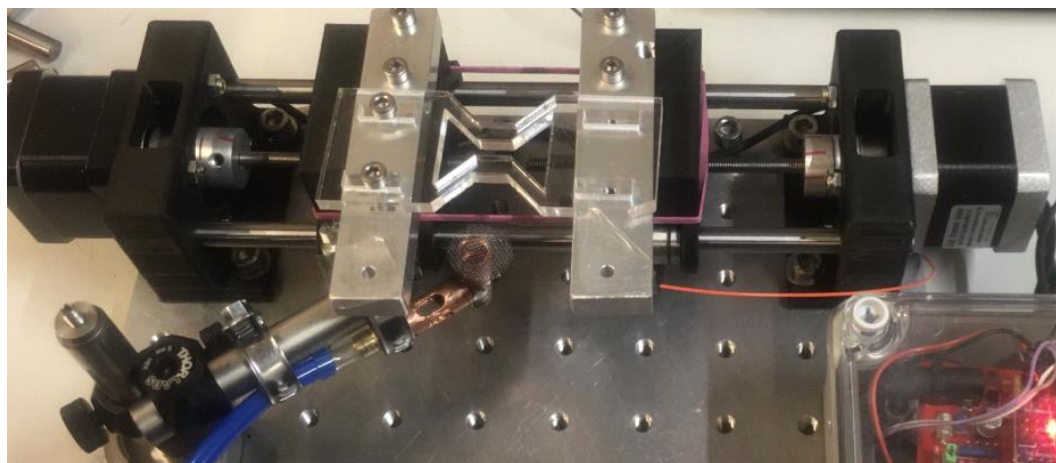
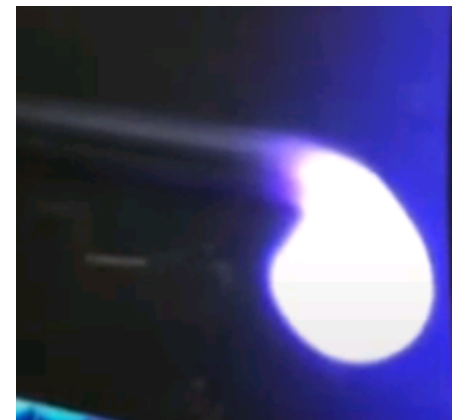
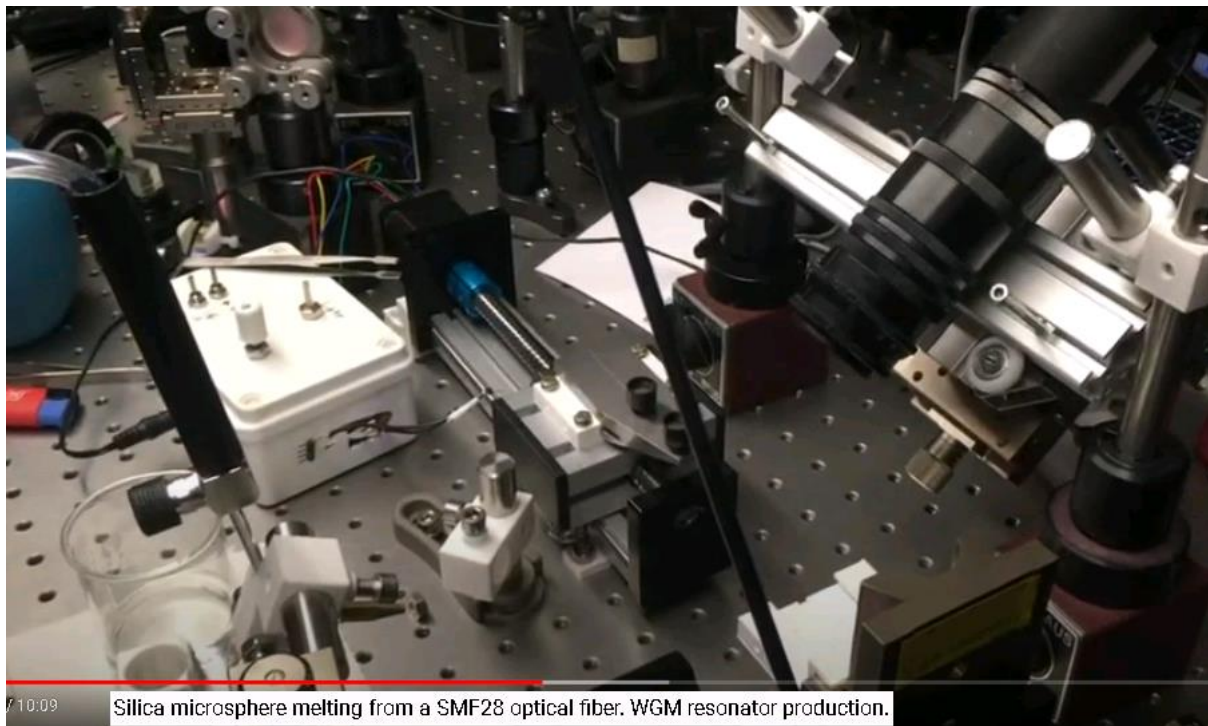
Free spectral range:
 $FSR = c / 2 \pi n R$

Example: 1mm sphere with Q factor 10^8 .
Light photons run 25 m inside until decay
due to scattering and absorption.



T1.1. Microsphere fabrication in oxy-hydrogen flame

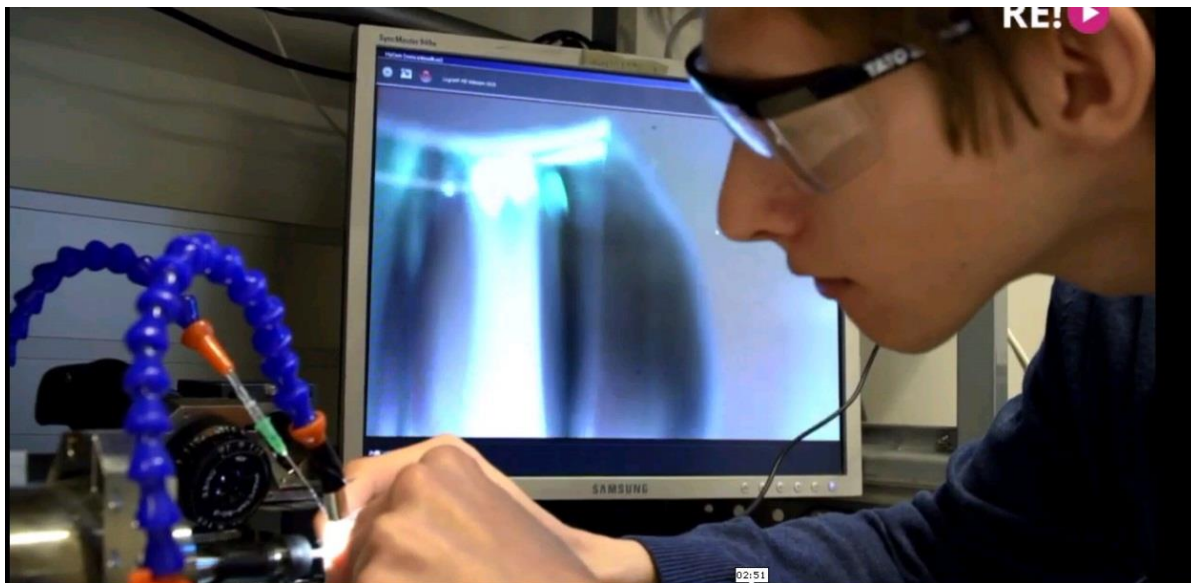
T1.3. Tapered fiber pulling in pure hydrogen flame



T1.1. Grinding and polishing of resonators with abrasives on air-bearing spindle. **Disadvantage : time consuming!**

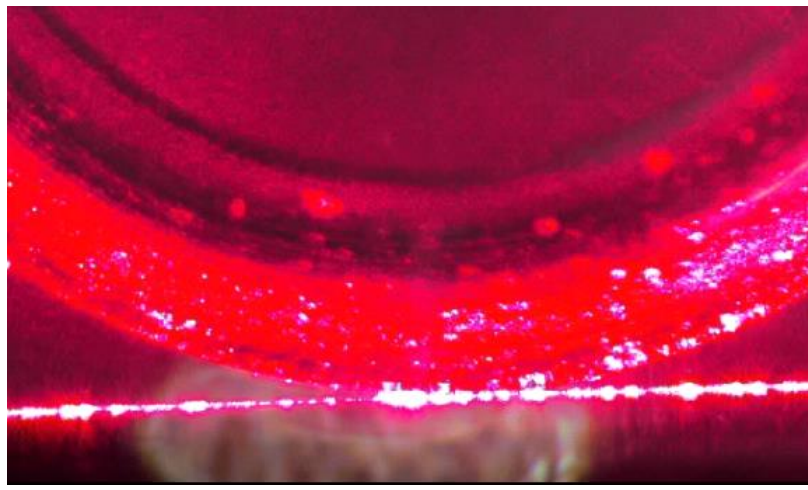
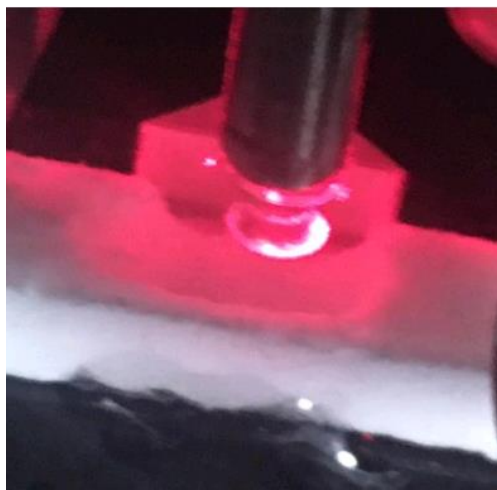
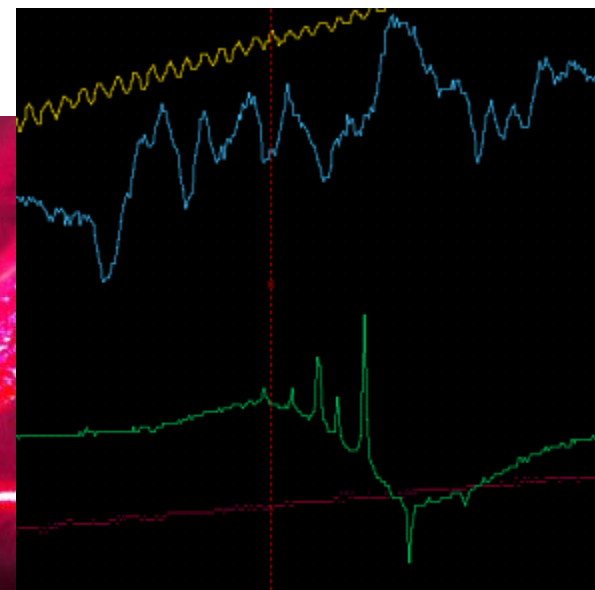
Materials CaF_2 , MgF_2 plexiglass, fused silica.

Diamond abrasives



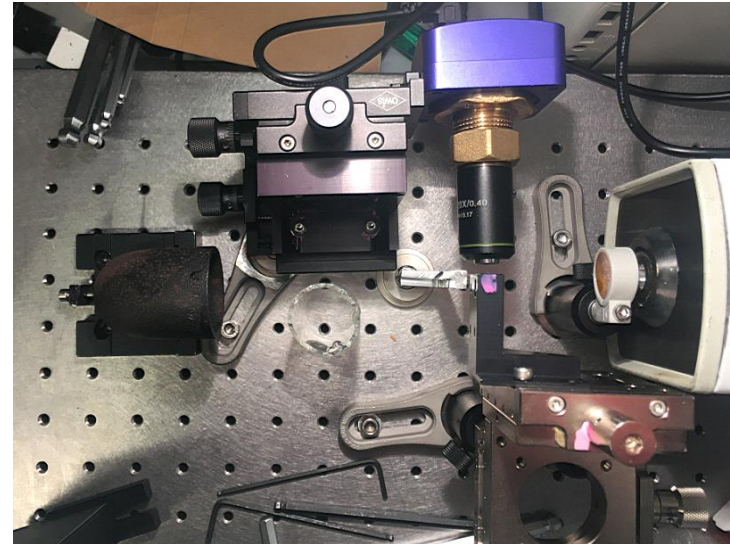
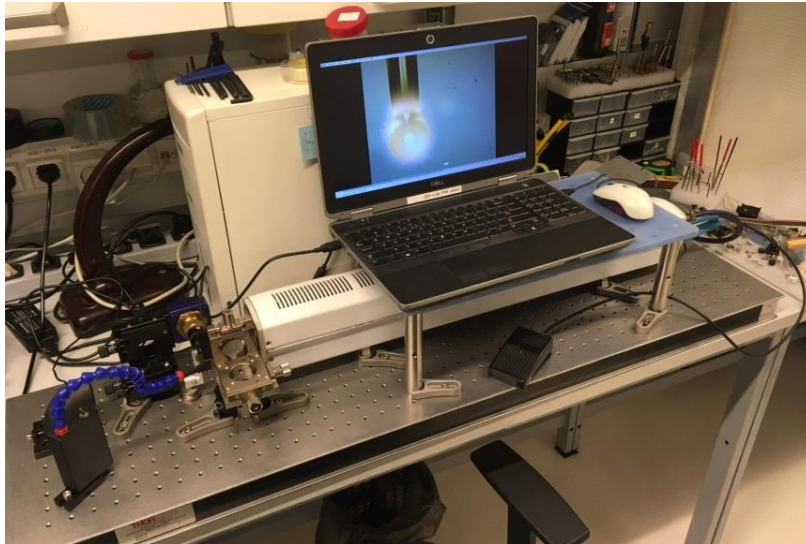
Prism and tapered fiber coupling

resonances →



T1.1. Microsphere and microrod fabrication with a 40W CO₂ laser lathe.

Most novel method. **Needs in future motorised CNC control.**

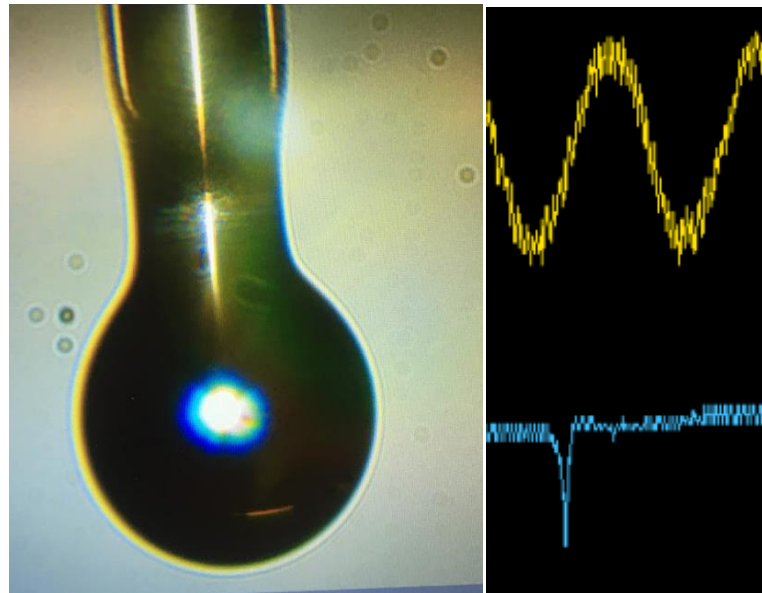


Home-made microscope:
20x objective from Ebay (60 EUR) and Astronomy webcam (150 EUR)

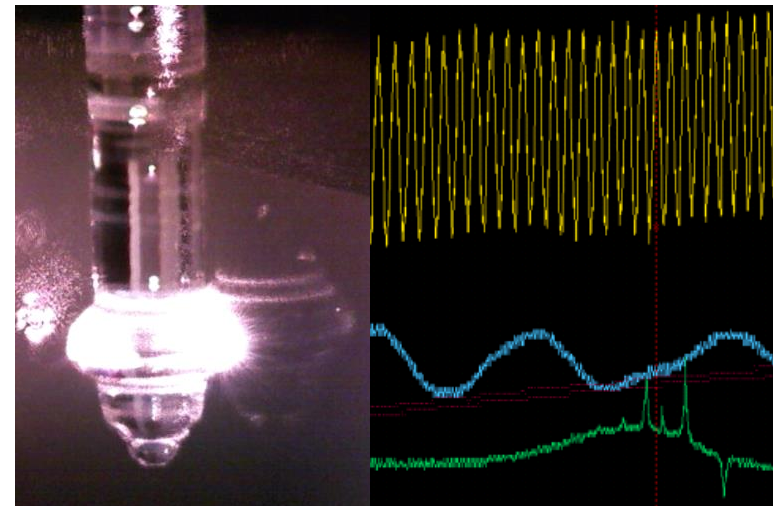
Sphere WGMR FWHM = 2 MHz **Q = 2E8 at 780 nm**

Microrod CO₂ lathe first resonances $Q \sim 10^6$.

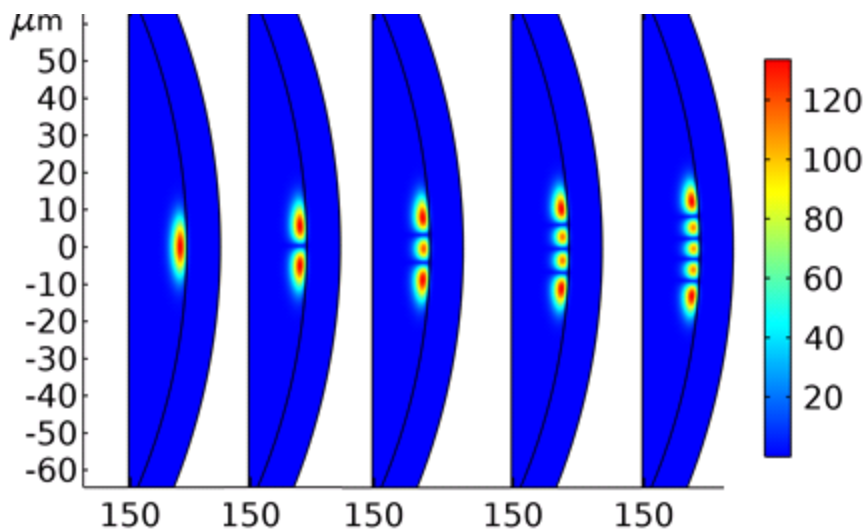
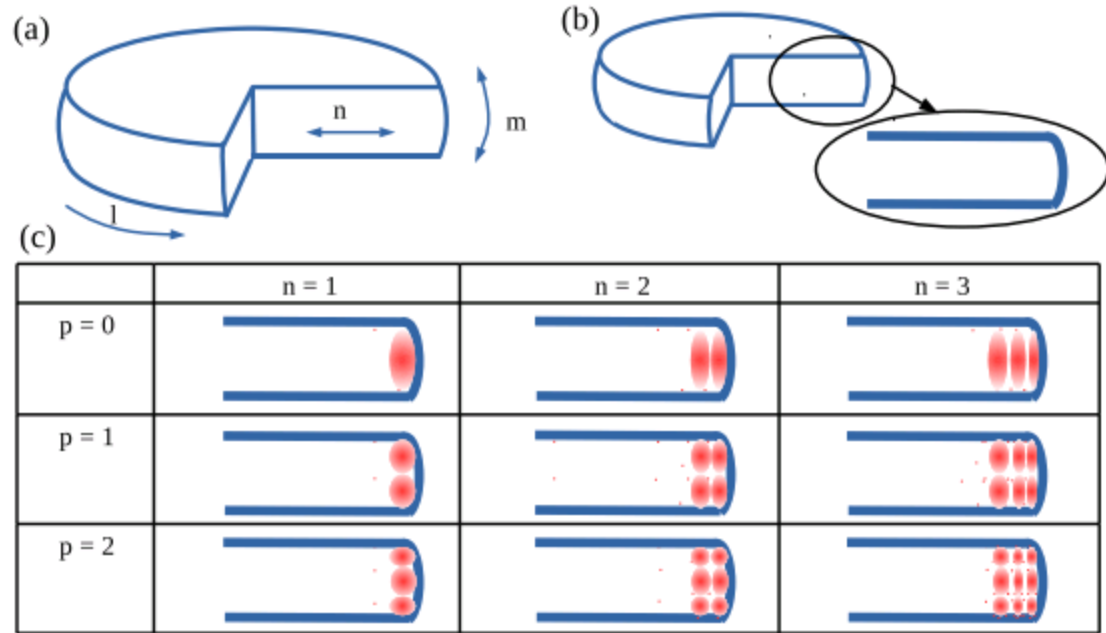
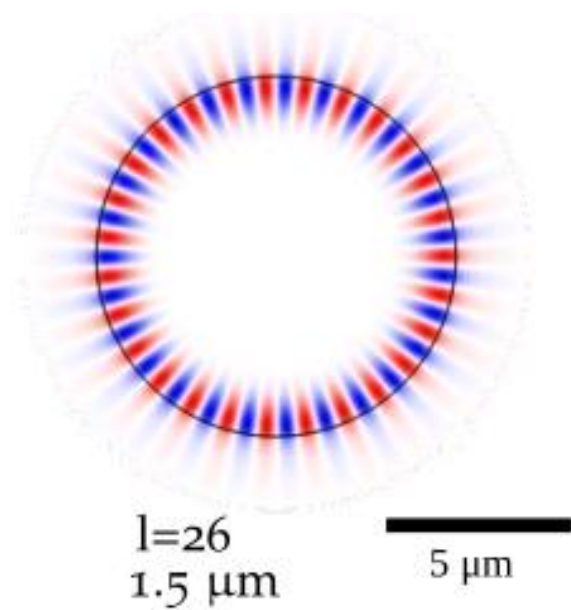
Evaporated silica dust is a problem



Yellow reference interference fringes from fiber etalon have 50 MHz period.



T1.4. Wave optics modeling of optical modes in COMSOL Multiphysics software



Understanding different WGMs: (a) radial mode number n , azimuthal mode number l and polar mode number m directions; (b) the region for plane sliced from a microsphere WGM resonator and (c) the intensity distributions for various modes in the slice.

Kerr effect - optical materials slightly change their index of refraction at large light intensities.

For Kerr effect (modifying the index of refraction) intensities $\sim 1 \text{ GW/cm}^2$ are necessary

Kerr effect has been usually observed with pulsed lasers

In microspheres it is possible with a CW laser

Peak intensity and circulating power calculations

power circulating
$$P_{circ} = P_{in} Q \frac{\lambda}{\pi^2 n R} \frac{K}{(1+K)^2}$$

Mode areas A_{eff} obtained from Comsol simulation

λ is the resonance wavelength, R is the device radius.
 Q is the quality factor of the device,
 n is the effective refractive index
 K is the coupling coefficient

Power and optical intensity circling inside the WGMR from 0.1 W input laser power.

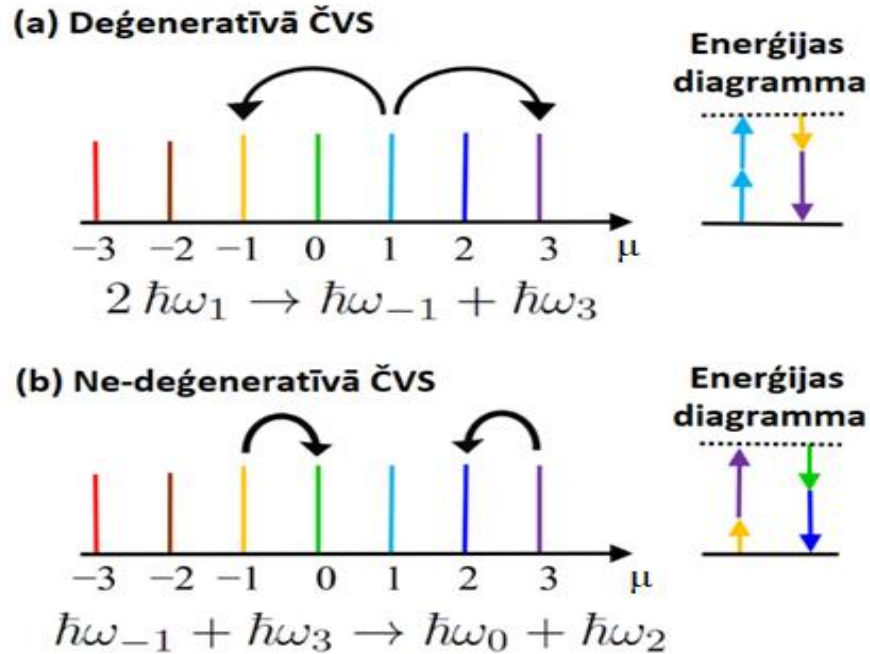
transmission:
$$T = \frac{(1-K)^2}{(1+K)^2}$$

intensity circulating
$$P_{circ}/A_m,$$

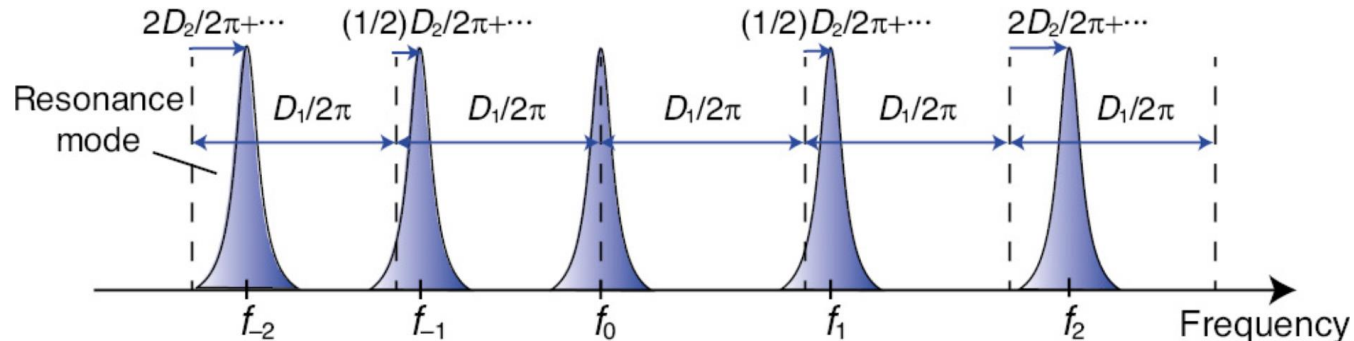
mode area
$$A_m = \frac{\int \epsilon(r) |E|^2 dA}{\max(\epsilon(r) |E|^2)}$$

R, μm	Q $\cdot 10^7$	T	K	Q_{intr} $\cdot 10^7$	P_{circ} W	$A_{eff},$ μm^2	$I_{circ},$ GW/cm^2
135	2.0	0.17	1.69	5.4	1016	36.15	2.8
60	1.2	0.26	2.05	3.7	1468	18.45	8.0
85	4.6	0.54	3.89	22.0	4671	24.62	19.0
83	5.2	0.14	1.61	13.6	4217	24.14	17.5

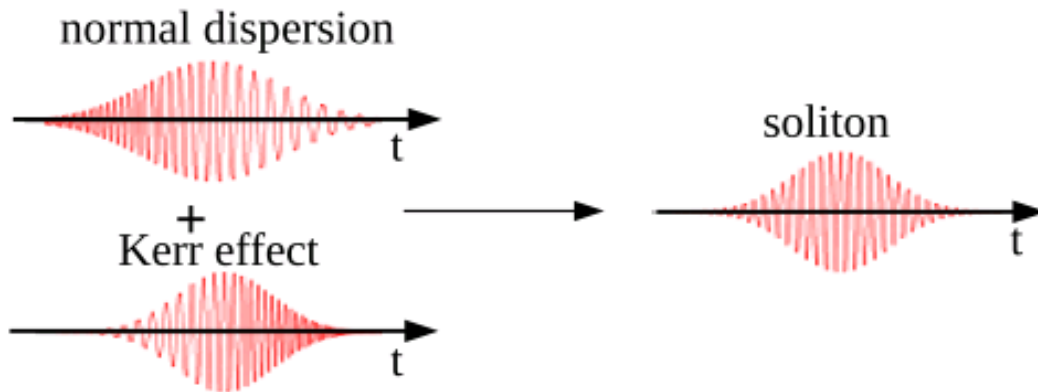
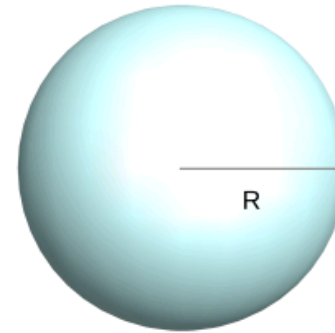
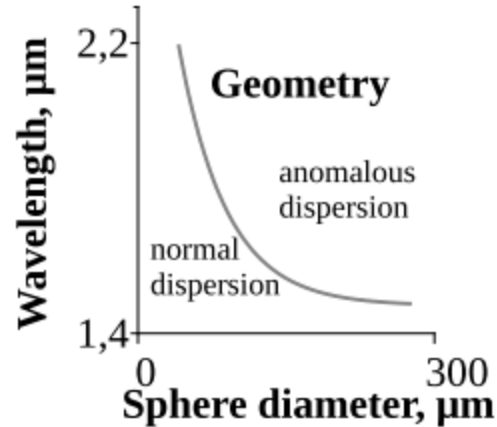
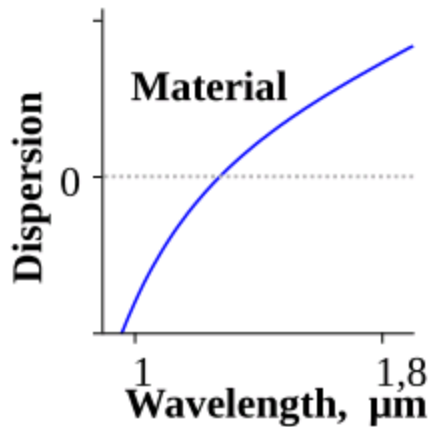
Four Wave mixing (FWM) nonlinear process



Dispersion caused detuning between comb and WGM lines



Material and geometrical dispersion depending on microsphere size



In soliton regime Kerr effect compensates dispersion. In such case dispersion is 0 and pulse circulates without changing length.

Soliton regime is the most stable regime, hard to get.

We have not been able to achieve soliton regime in microspheres because of microsphere heatup and the tunable laser that we have does not have large enough wavelength scan

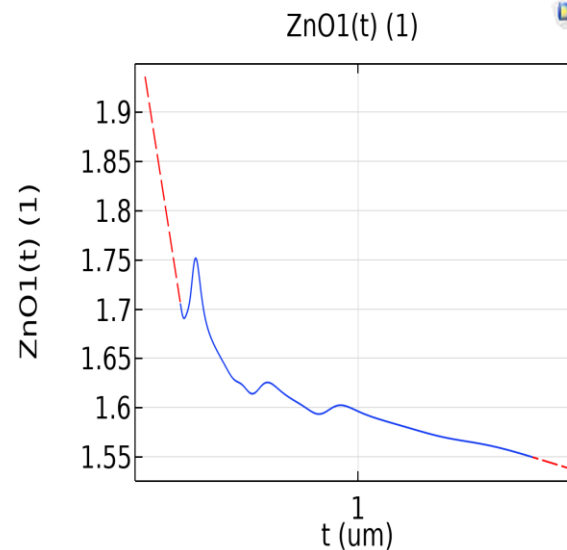
COMSOL Multiphysics lietojums dispersijas aprēķināšanai

apbrīnāšanai

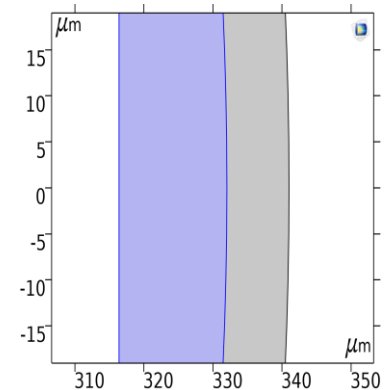
Rezonatora materiāla uzdošana

- Uzdod materiālās dispersijas datu tabulu
- Izveido interpolācijas funkciju $n=n(\lambda)$
- Uzdod materiāla apgabala gaismas laušanas koeficientu kā funkciju $n(\lambda)$.

→ Rēķinot pie dažādām frekvencēm tiek ņemtas dažādas n vērtības



Variables	
Name	Expression
n	SiO2(ewfd.lambda0)
ZnO11	ZnO1(ewfd.lambda0)
ZnO22	ZnO2(ewfd.lambda0)



Property	Variable	Value	Unit	Property group
<input checked="" type="checkbox"/> Refractive index, real part	n_iso ;...	ZnO11	1	Refractive index
<input checked="" type="checkbox"/> Refractive index, imaginary part	ki_iso ;...	0	1	Refractive index

Dispersijas aprēķins

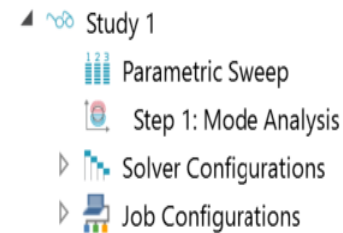
- COMSOL Multiphysics aprēķina n_{eff} izmantojot Mode Analysis

- Pēc formulas $2\pi Rn = m\lambda$ aprēķina m

- MATLAB no tabulas uzdod $\omega = \omega(m)$ [rad/s]

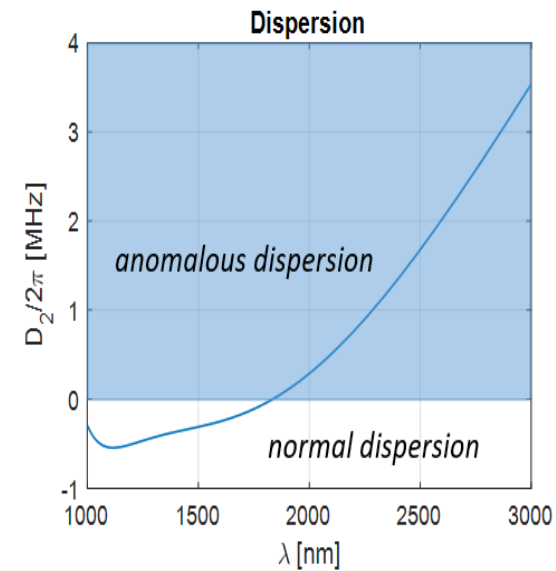
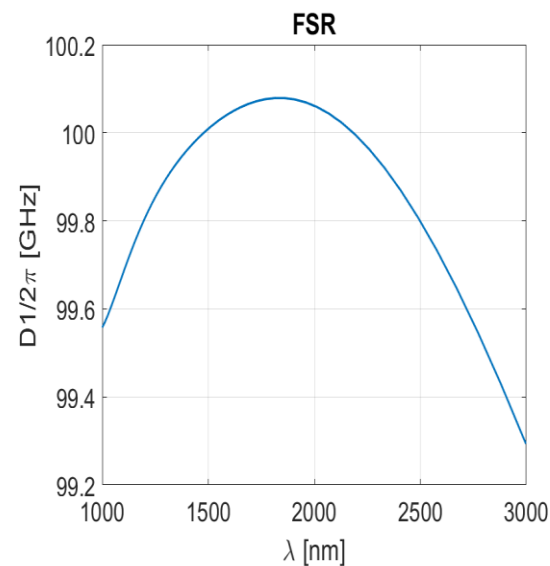
- Aprēķina $FSR = \frac{\partial \omega}{\partial m} \frac{1}{2\pi}$ [Hz]

- Dispersija $D_2 = \frac{\partial^2 \omega}{\partial m^2}$ [rad/s]

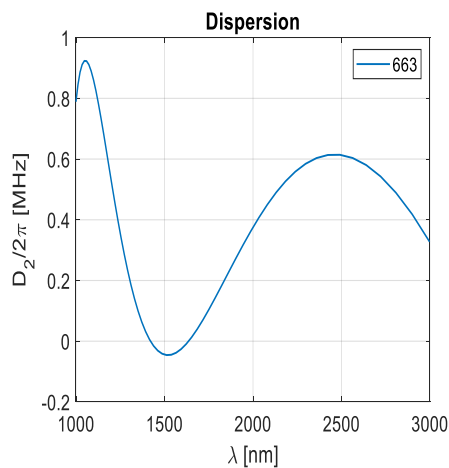
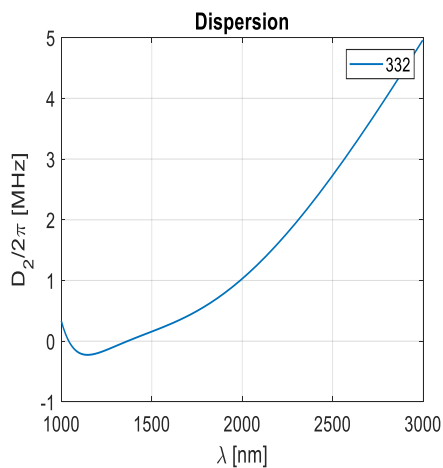
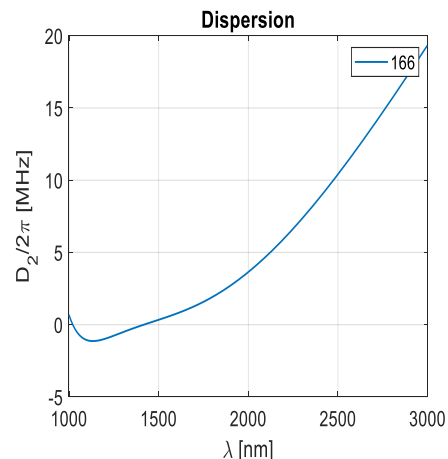
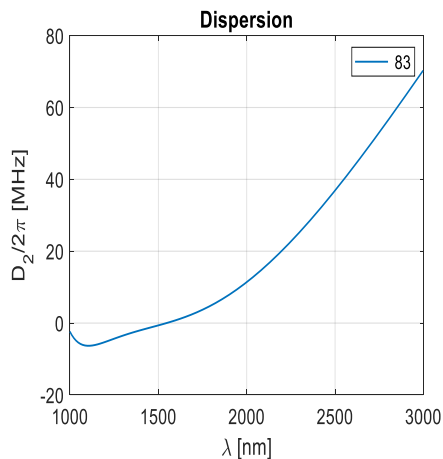
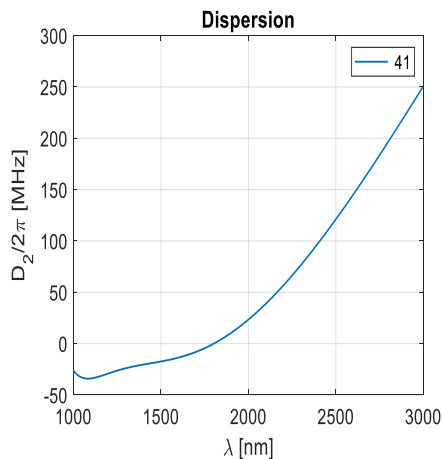


Sweep type: All combinations

Parameter name	Parameter value list	Parameter unit
freq1	range(1.5e14,2.542372881355932e12,3.0e14)	Hz



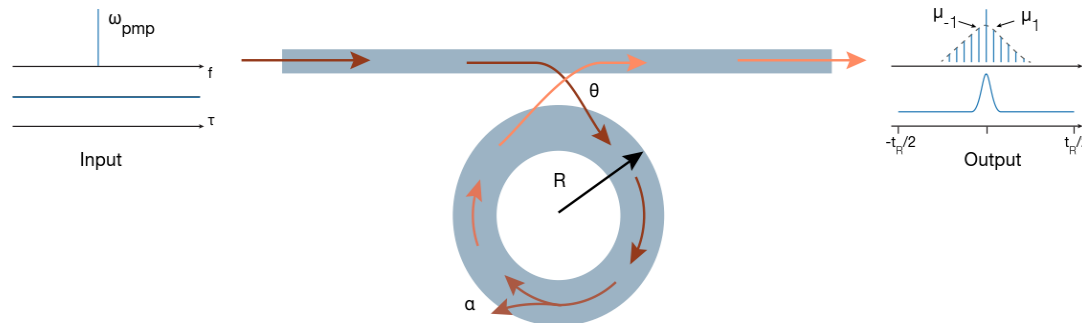
Nulles dispersijas viļņa garums dažādu izmēru SiO₂ sfērām



R, μm	FSR, GHz	ZDW, nm
41	800	1802
83	400	1545.6
166	200	1417.4
332	100	1041.3 & 1364.7
663	50	1421 & 1635

Lugiato-Lefevēra vienādojuma modelēšana

- Ar brīvpieejas programmatūru **pyLLE** (Python>3.4, Julia 0.6.4)
- [Moille G, Li Q, Lu X, Srinivasan K (2019) pyLLE: A Fast and User Friendly Lugiato-Lefever Equation Solver. J Res Natl Inst Stan 124:124012.
[https://doi.org/10.6028/jres.124.012.](https://doi.org/10.6028/jres.124.012)]



$$t_R \frac{\partial E(t, \tau)}{\partial t} = - \left(\frac{\alpha'}{2} - i\delta_0 \right) E + i \cdot \text{FT}^{-1} \left[-t_R D_{\text{int}}(\omega) \cdot \text{FT} [E(t, \tau)] \right] + \gamma L |E|^2 E + \sqrt{\theta} E_{\text{in}}$$

- kur integrālā dispersija ir $D_{\text{int}} = \omega_{\mu} - (\omega_0 + D_1 \mu)$

pyLLE

Please note that if you are using this notebook, you need to make sure that you "trust" it to ensure the display of the figure. To do so, in the jupyter notebook, go to File → Trust this notebook. It should reload the notebook and the plotly figure will be able to be displayed now

Import and Setup

In a python shell, spyder, a script, or in jupyter notebook, start by importing the package.

```
In [42]: import pyLLE
```

We now define the resonator parameters. Here we will use a file `TestDispersion.csv` which is made of two columns: the first one is the azimuthal mode order (integer), the second is their corresponding frequency of resonance in Hz.

```
In [43]: res = {'R': 327e-6, # ring radius in meter
              'Qi': 1e7, # Intrinsic Q factor
              'Qc': 1e7, # Coupled Q factor
              'gamma': 1.55, # Non-linear coefficient at the pump frequency
              'dispfile': 'TestDispersion.csv', # frequency and corresponding azimuthal mode simulated previously
              }
```

We now define the simulation parameters. Here we precise a linear detuning ramp of the pump from ω_{init} to ω_{end} relative to the pump mode angular frequency, mode closest to the defined pump frequency f_{pmp} . The simulation length `Tscan` is in unit of round trip, as it is more convenient in the Lugiato-Lefever formalism. It is important to notice that two parameters for the mode bandwidth have to be defined, μ_{fit} which determined the fit window of the raw data found in `dispfile`, and μ_{sim} which is the number of mode simulated in the LLE, hence could be larger than the fit mode through extrapolation

```
In [44]: import numpy as np
sim = {'Pin': 150e-3, # Input power in Q
      'Tscan': 1e7, # Length of the simulation in unit of round trip
      'f_pmp': 193479318217425, # Pump Frequency
      'omega_init': 2e9*2*np.pi, # Initial detuning of the pump in rad/s
      'omega_end': -10e9*2*np.pi, # End detuning of the pump in rad/s
      'mu_sim': [-60, 60], # azimuthal mode to simulate on the left and right side of the pump
      'mu_fit': [-60, 60], # azimuthal mode to fit the dispersion on the left and right side of the pump
      }
```

In both the resonator and simulation dictionaries, the parameters can be called through their greek letters or through their equivalent latin names (e.g. $\mu \rightarrow \mu$ or $\delta\omega \rightarrow \text{deltaomega}$). A translator dictionary is implemented to translates every greek entries (see: `self_greek`)

Simulation Parameters:

$R = 327.00 \mu\text{m}$

$Q_i = 10.00 \text{ M}$

$Q_c = 10.00 \text{ M}$

$\gamma = 1.55$

$P_{in} = 150.00 \text{ mW}$

$T_{scan} = 10.00 \times 10^6 \text{ Round Trip}$

$f_{pmp} = 193.48 \text{ THz}$

$\omega_{init} = 2.00 \times 2\pi \text{ GHz}$

$\omega_{end} = -10.00 \times 2\pi \text{ GHz}$

$\mu_{sim} = [-40.00, 40.00]$

$\mu_{fit} = [-40.00, 40.00]$

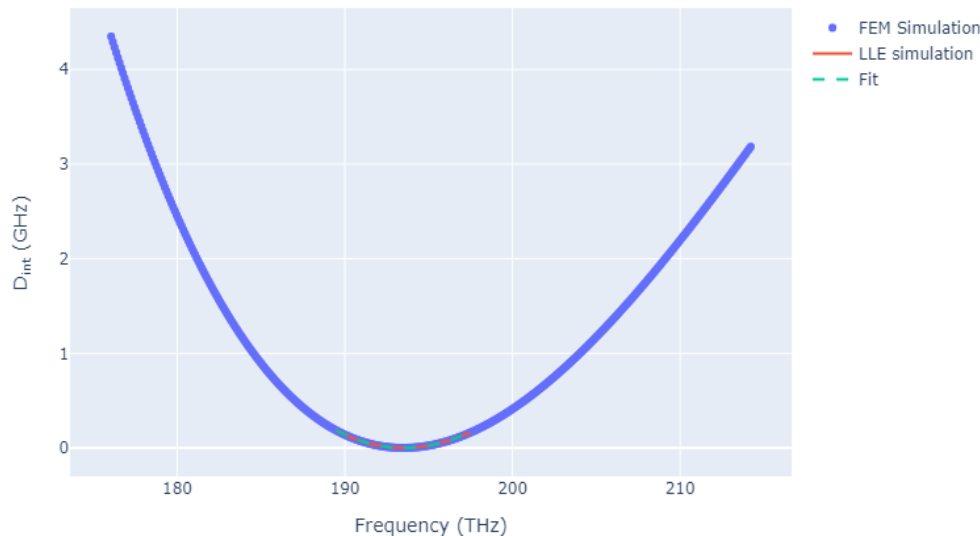
pyLLE

- Programmā tiek ielikts iepriekš, citur aprēķināts atbilstošā rezonatora modu un frekvenču lielumus, piemēram ar Sellmeiera vienādojumi:

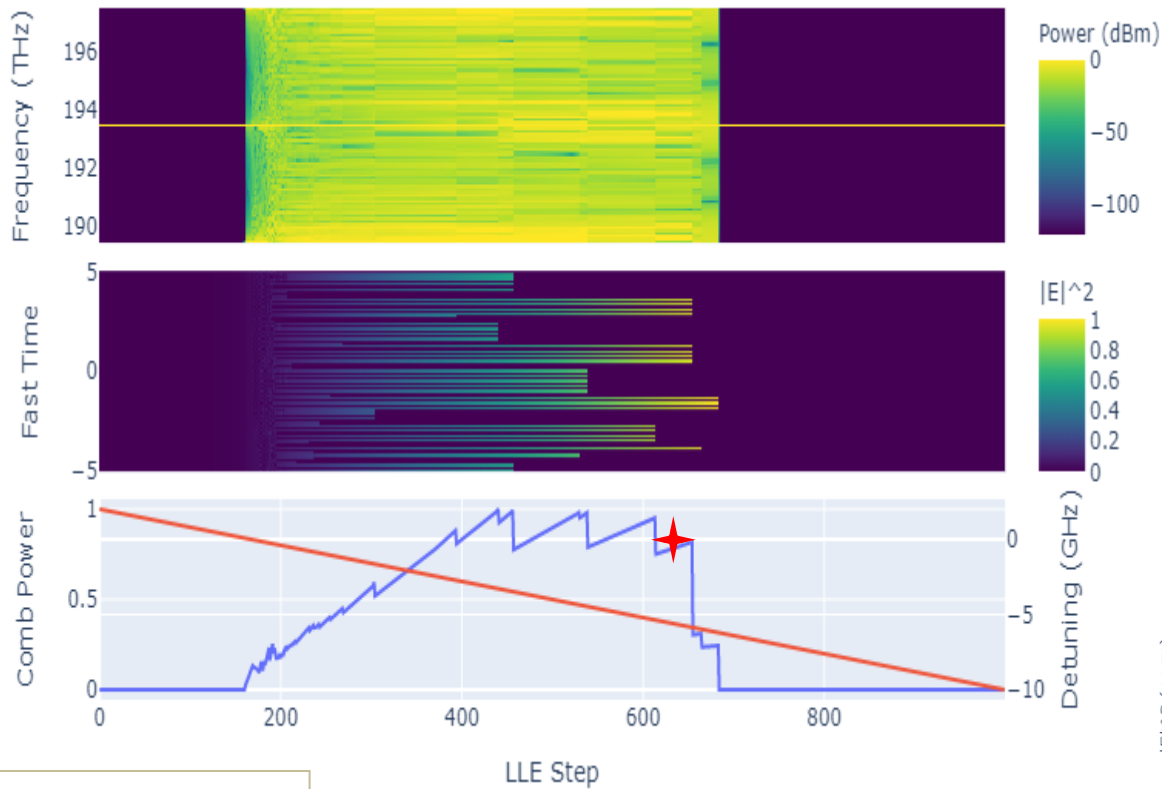
$$\lambda_{TE} \approx \frac{2\pi R n_1}{m + 1.856m^{\frac{1}{3}} + \left(\frac{1}{2} - \frac{n_1}{\sqrt{n_1^2 - 1}} \right)}$$

$$n^2(\lambda) = 1 + \sum_i \frac{A_i \cdot \lambda^2}{\lambda^2 - B_i^2},$$

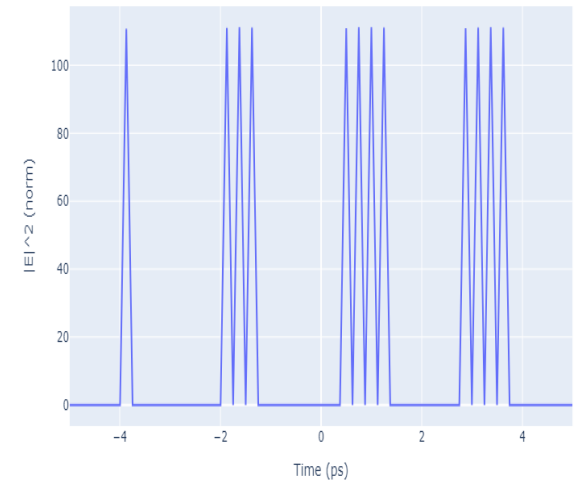
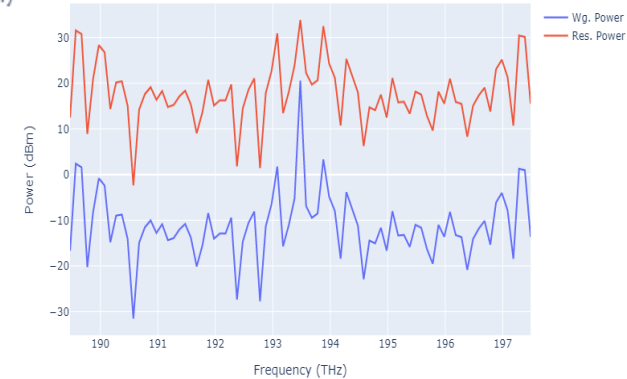
- Tiek aprēķināta integrālā dispersija



pyLLE – rezultātā iegūstam mikroķemmes uzvedību kā spektru, frekvenču ķemmes jaudu rezonatorā pie dažādiem LLE soļiem, kā arī pie noteiktiem soļiem redzam rezonatora elektriskā lauka spektru un sadalīumu laikā.



ind=630

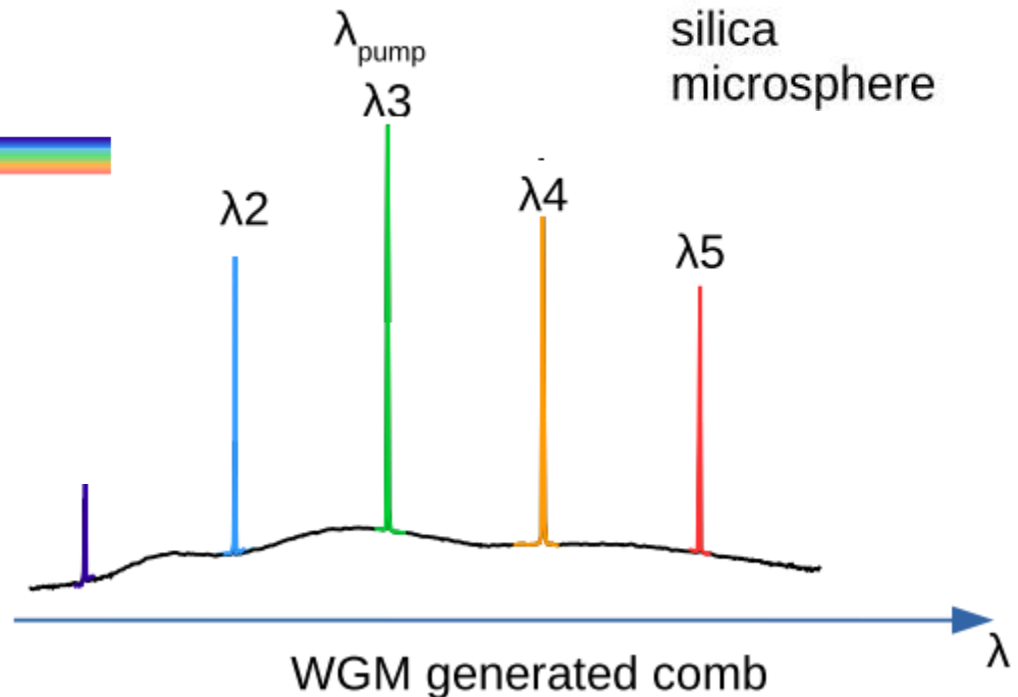
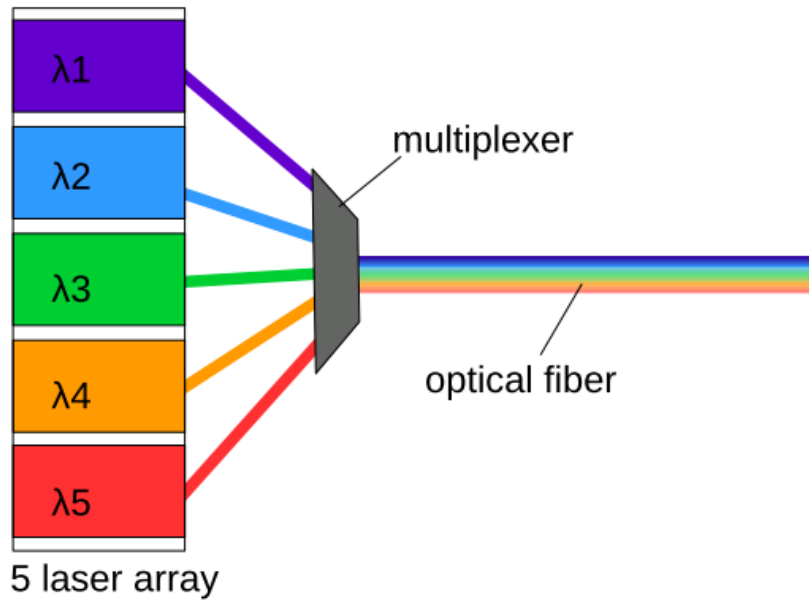


$R = 327.00 \mu\text{m}$
 $Q = 10.00 \text{ M}$
 $\mu = [-40.00, 40.00]$
 Center Pump: 193.479
 THz
 FSR: 100.15 GHz

Future Vision of the Project outcome

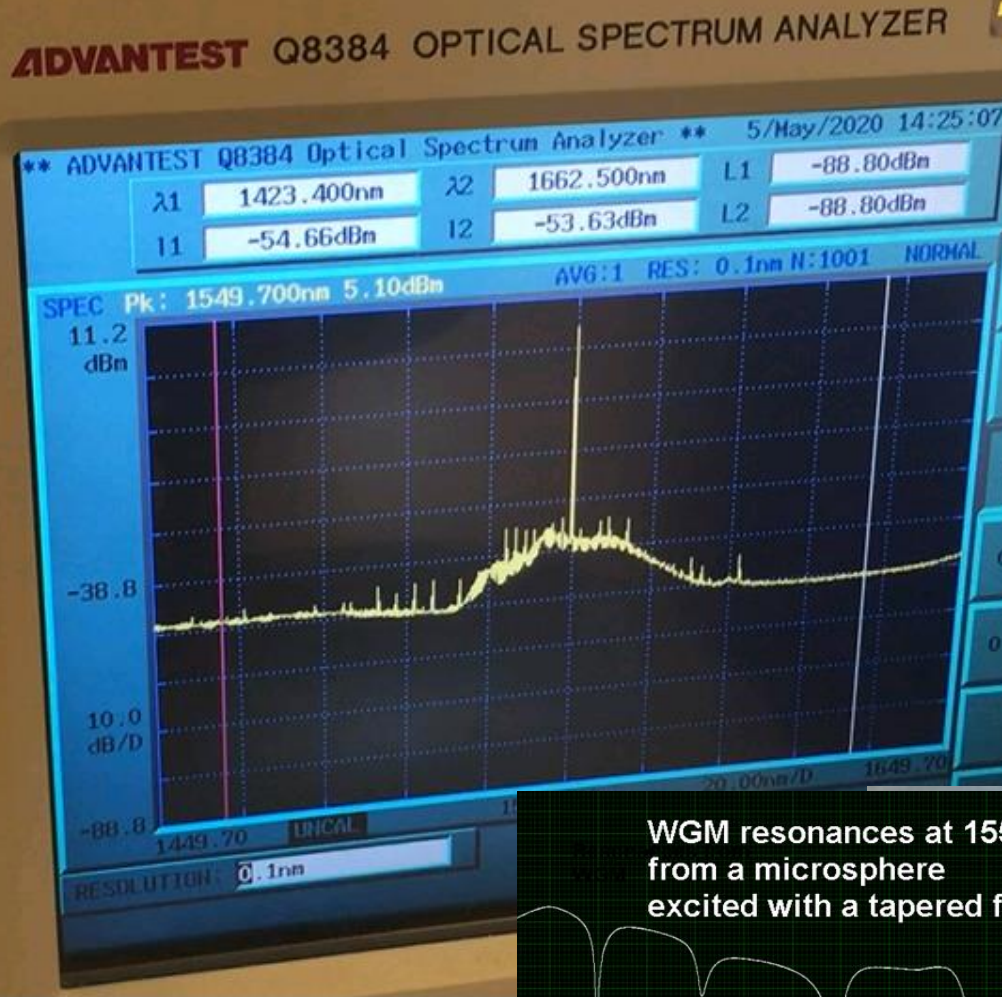
Wavelength Division Multiplexing

Replace laser array with frequency comb generated inside WGM resonator.

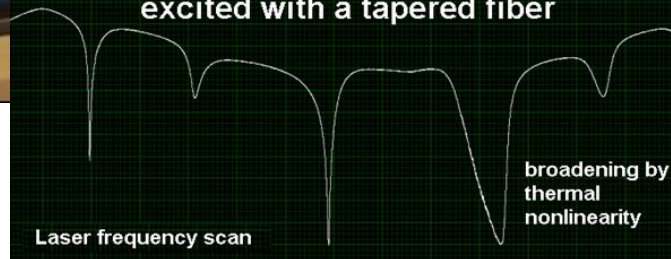


T1.3. May 2020. Our first comb from SiO₂ microsphere.

Weak and unstable in time because microsphere symmetry was deformed

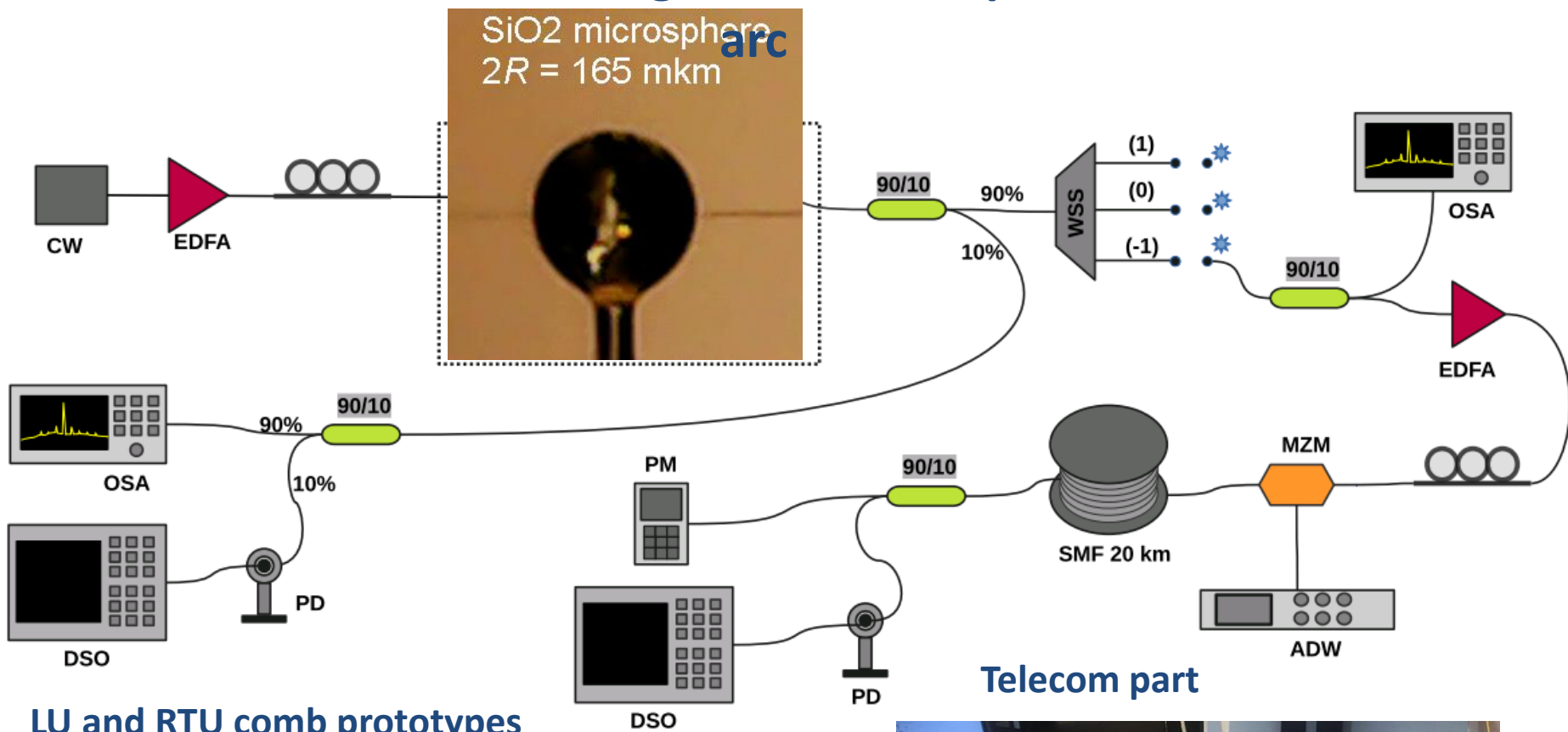


WGM resonances at 1550 nm from a microsphere excited with a tapered fiber

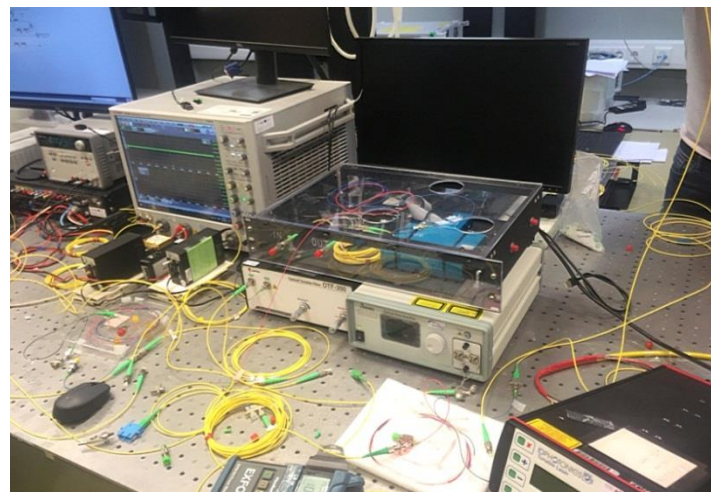
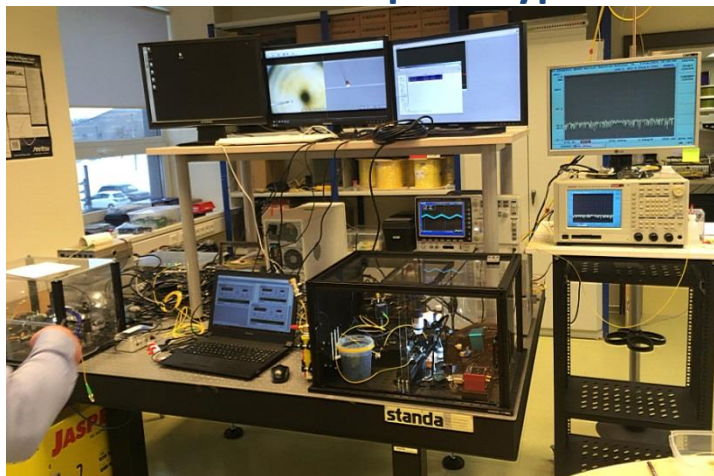


$$Q \approx 3 \times 10^7$$

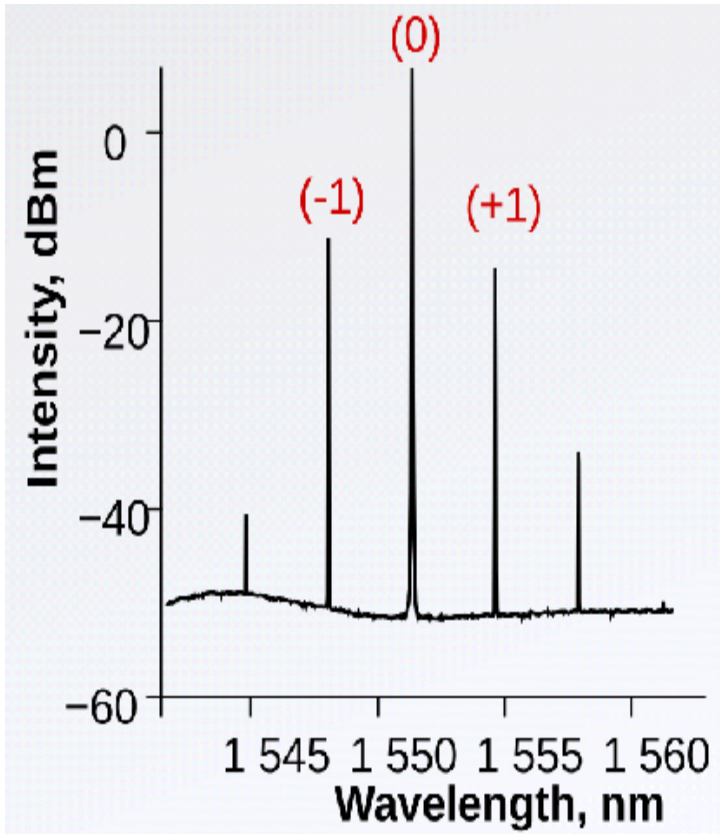
T2.1. Comb for telecom using round microsphere made in electric



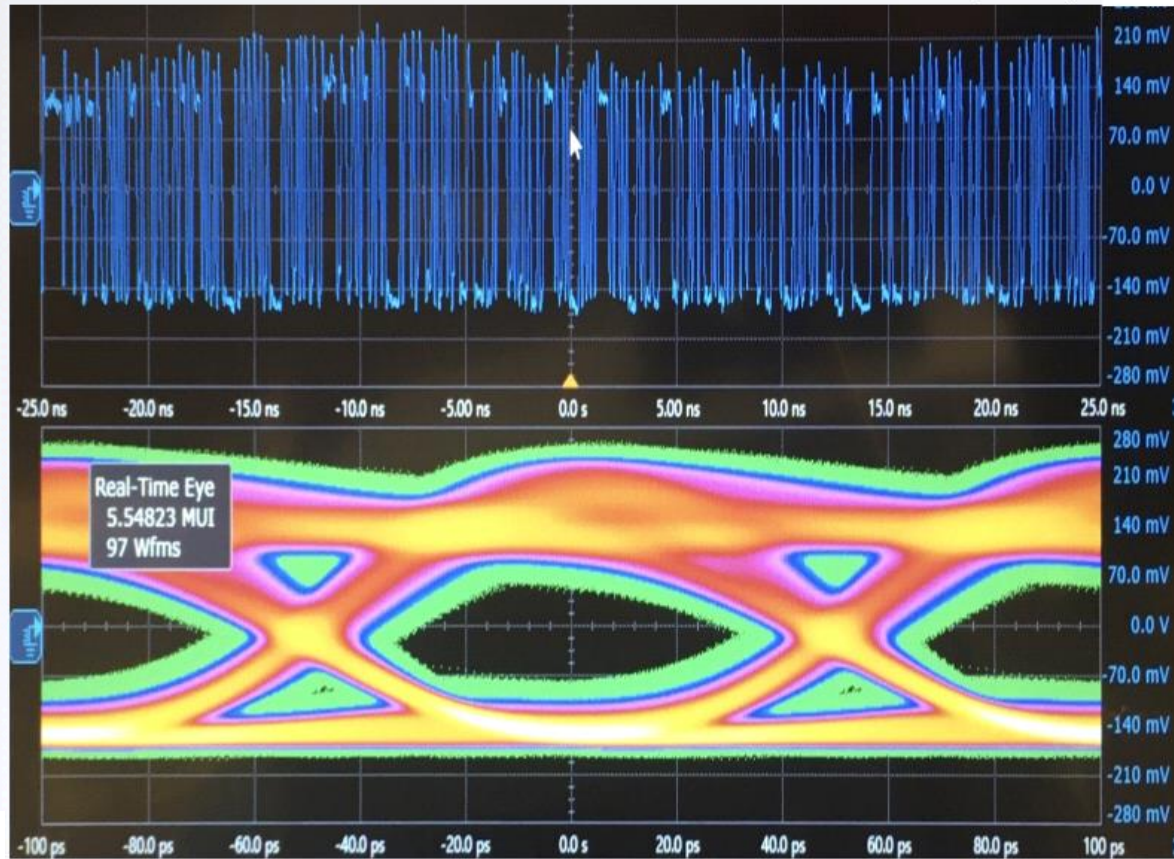
LU and RTU comb prototypes



Comb for telecom result



10 Gbit/s data and eye diagram on WDM selected OFC line (+1)



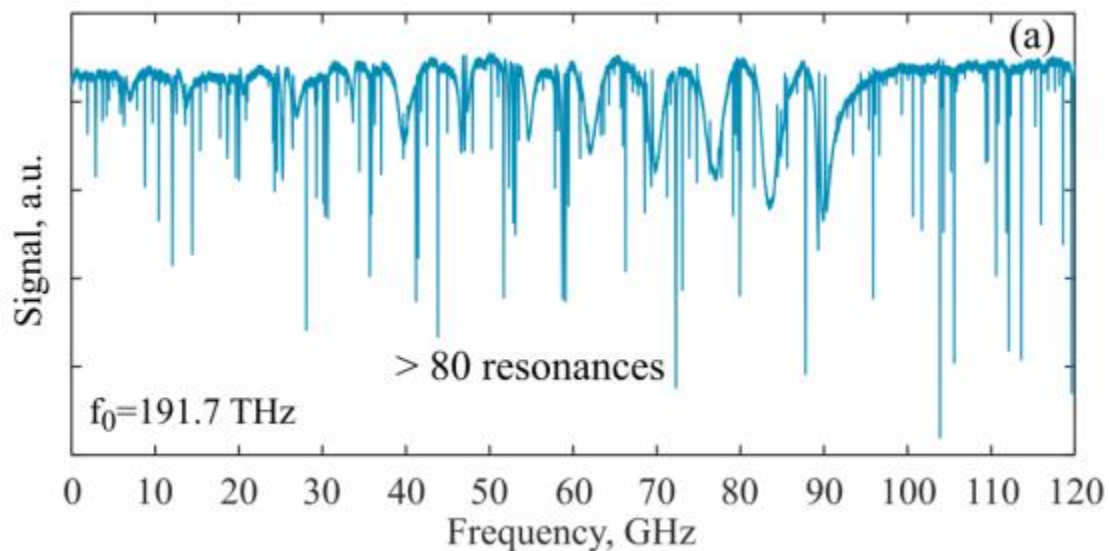
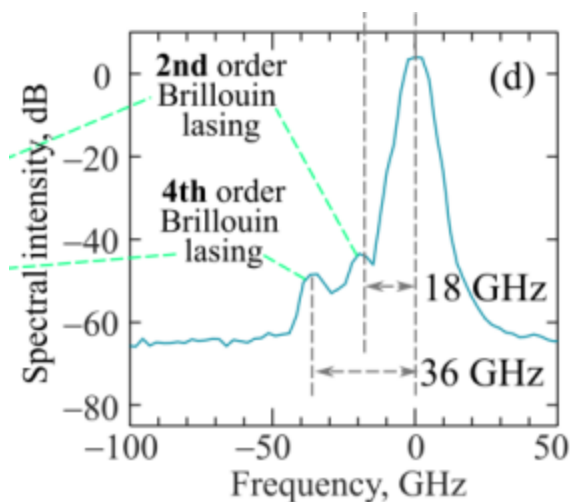
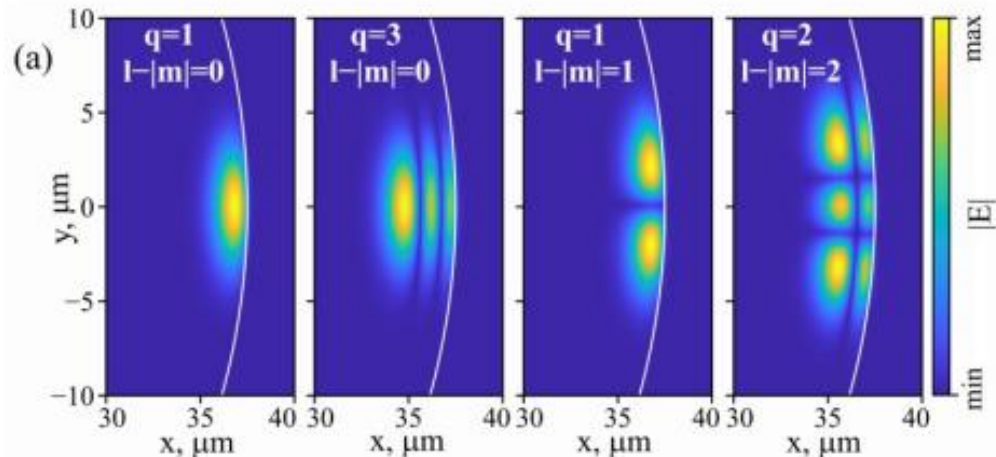
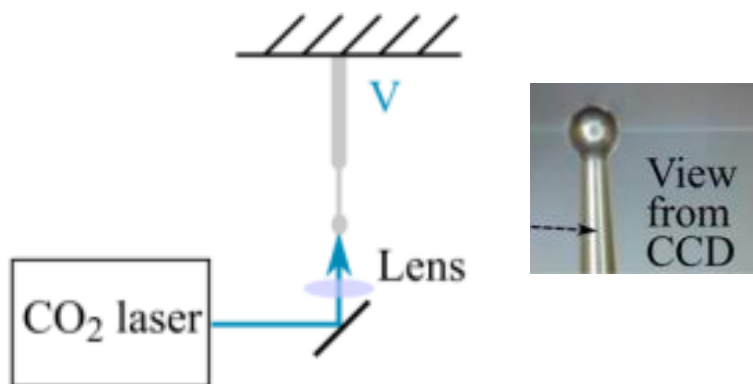
E.A. Anashkina, V. Bobrovs, T. Salgals, I. Brice, J. Alnis, A.V. Andrianov,
Kerr optical frequency combs with multi-FSR mode spacing in silica microspheres
IEEE Photonics Technology Letters 33, 453-456 (2021).

T. Salgals, J. Alnis, R. Murnieks, I. Brice, J. Porins, A. V. Andrianov, E. A. Anashkina, S. Spolitis, V. Bobrovs,
Demonstration of a fiber optical communication system employing a silica microsphere-based OFC source,
Optics Express 29, 10903-10913 (2021).

Importance of microsphere roundness: less mode splitting spectral lines

Cascade Brillouin Lasing in a Tellurite-Glass Microsphere Resonator with Whispering Gallery Modes *sensors*

Elena A. Anashkina ^{1,*}, Maria P. Marisova ¹, Vitaly V. Dorofeev ^{1,2} and Alexey V. Andrianov ¹



Importance of microsphere roundness: less mode splitting spectral lines

In an ideal microsphere for a given l , modes with different azimuthal indices m , $-l \leq m \leq l$ are degenerate. This degeneracy is lifted if the microresonator is deformed. The resulting mode splitting can be described by the perturbation theory and, in the simplest case of a deformation into a spheroid, new eigenfrequencies can be found as follows [49]:

$$\frac{f_{l,m}}{f_l^{(0)}} = 1 - \frac{1}{3}\eta \left(1 - 3\frac{m^2}{l(l+1)} \right) \quad (3)$$

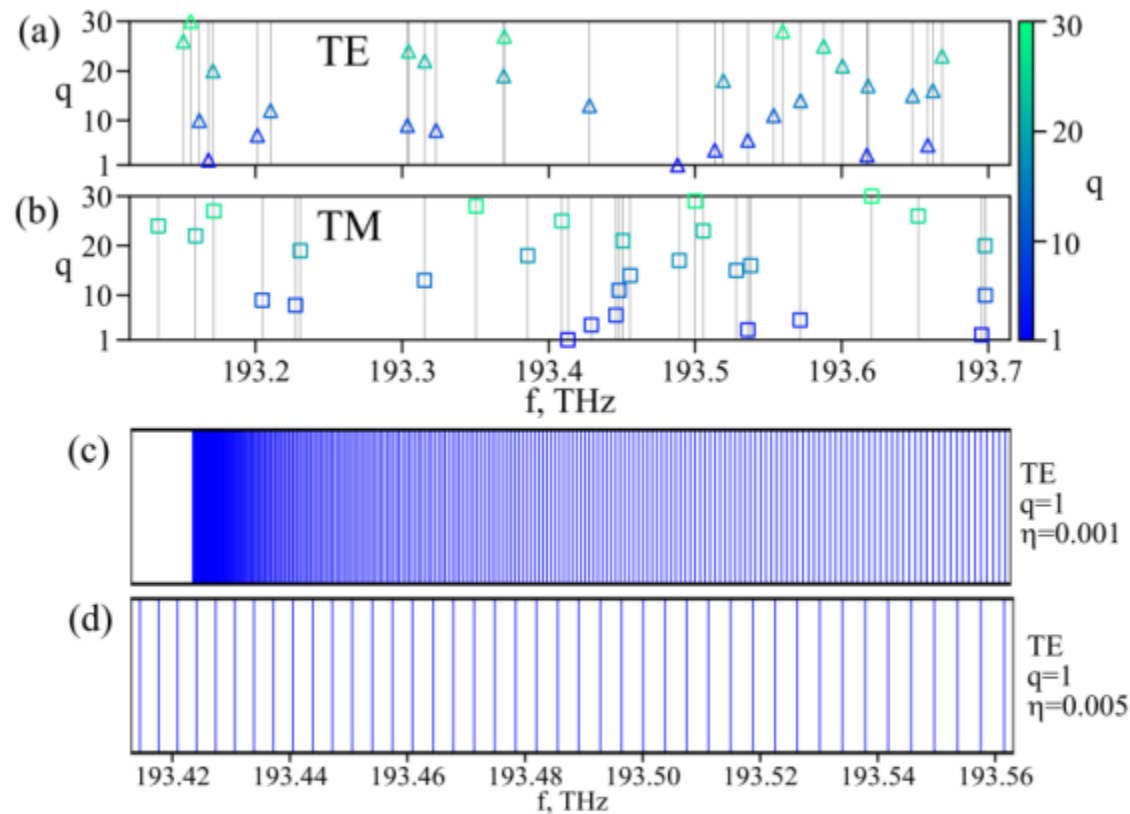


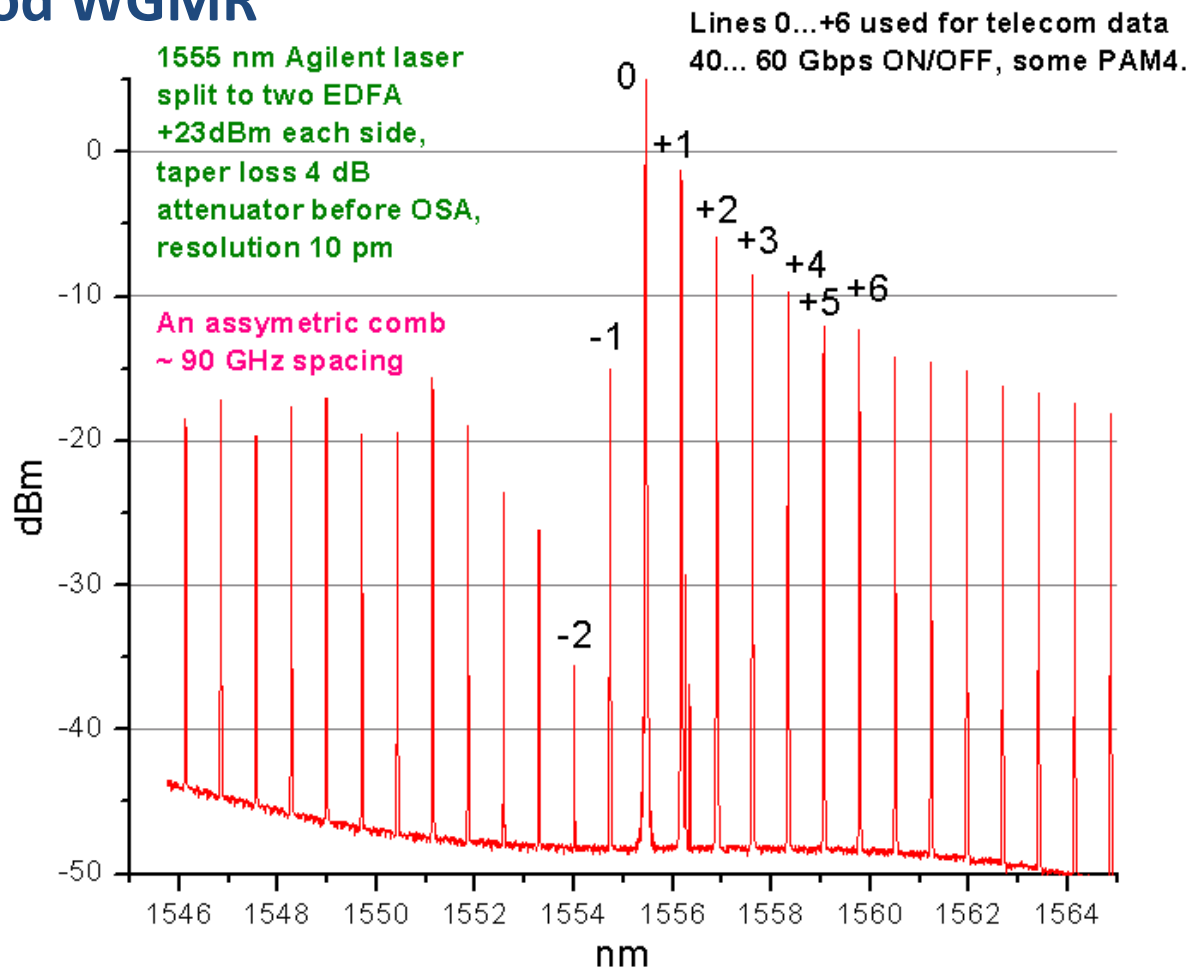
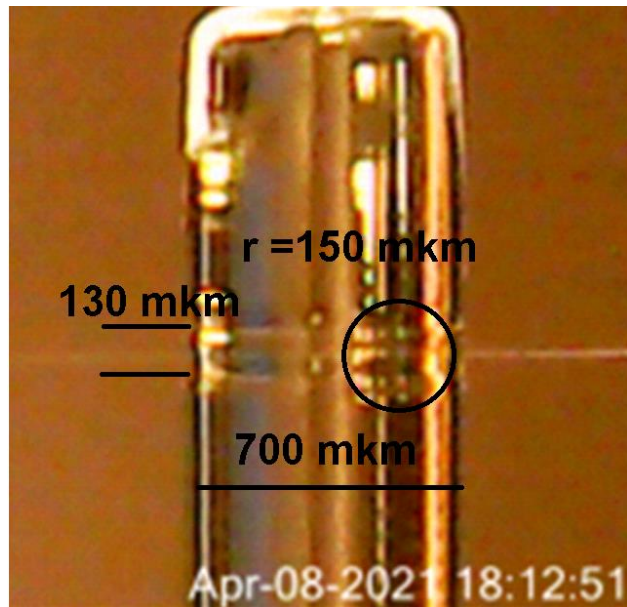
Figure 8. Eigenfrequencies of ideal 75 μm tellurite microsphere near $\lambda = 1.55 \mu\text{m}$ for TE (a) and TM (b) modes with different radial indices q ; vertical lines show resonance positions. Resulting splitting of the fundamental TE mode for microresonator with the shape-deformation parameter η defined based on Equation (3); $\eta = 0.001$ (c), $\eta = 0.005$ (d).

T1.3 and T2.1. SiO₂ microrod WGMR

made on a CO₂ laser lathe.

FSR optimised to 100 GHz.

Narrow rim limits the number of spatial modes.



Conclusions and outlook

Demonstration of World Record: 319 Tb/s Transmission over 3,001 km with 4-core optical fiber

- >120 nm signal bandwidth comprising 552 WDM channels and using both-doped fiber and Raman amplification - July 12, 2021 Japanese version

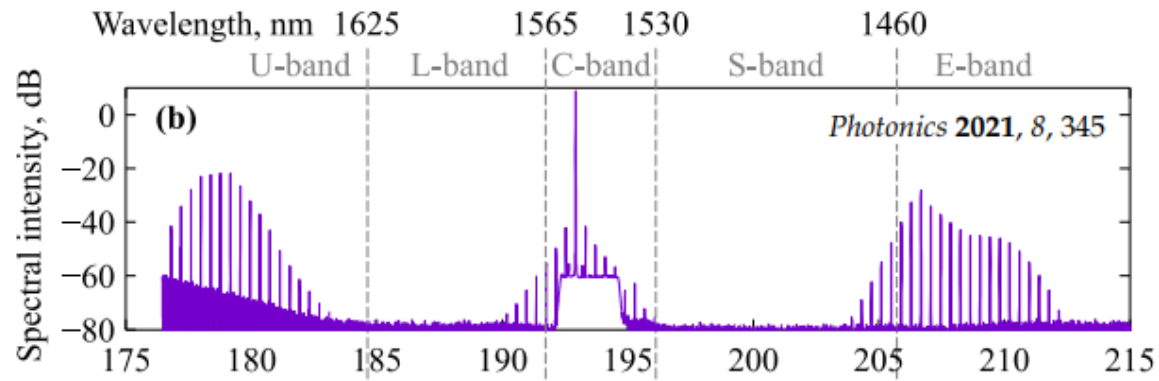
National Institute of Information and Communications Technology

Comb advantages:

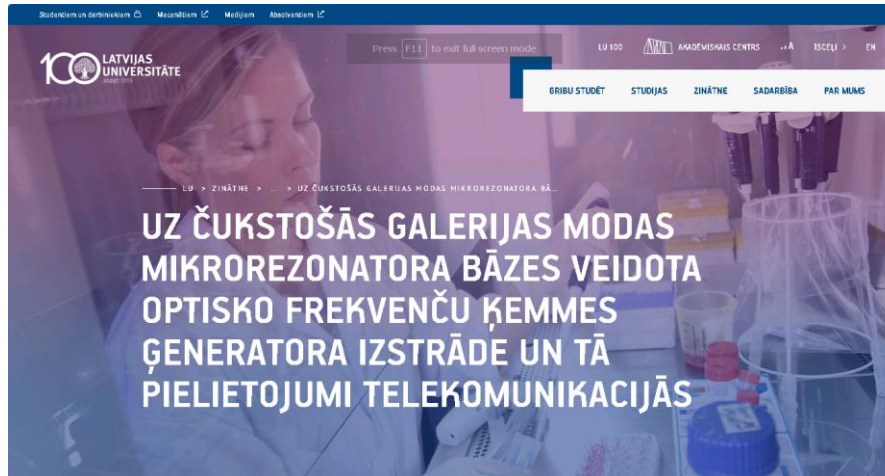
- Comb generated channel spacing is well defined and stable..
- In 2021 Japan demonstrated 300 TB/s telecom data transfer using 500 comb lines that would not be possible using 500 individual DFB lasers.

Comb disadvantages:

- Turing roll combs experience some amplitude instability. More stable soliton regime combs we could not get in microspheres do to dominating thermal effects.
- One needs to separate by filter individual comb lines before sending to data modulator.
- Comb lines have exponentially decreasing amplitude away from the pump. We could use only the few strongest lines. Telecom modulators are optimised for channel power of 1 mW (0 dBm).
- Pascal Del'Haye recommends us to filter out EDFA broadband noise and preamplify and level-out the comb lines with EDFA to telecom levels.



T4.5. WWW pages of the Project



www.rtu.lv/lv/universitate/projekti/atvert

ĀTRĀS SAITES LAPAS KĀRTE KONTAKTI ORTUS CĪTAS STRUKTŪRVIENĪBAS



Nāc studēt

Studijas

Zinātne

Valorizācija

Internacionalizācija

Universitāte

PROJEKTS

Sākums > Universitāte > Projekti

> Uz čukstošās galerijas modas mikrorezonatora bāzes veidota optisko frekvenču ķemmes ģeneratora izstrāde un tā pielietojumi telekomunikācijās



PAR UZŅĒMUMU

PROJEKTI

IEPIRKUMI

REKVIZĪTI

WCOMBS

UZ ČŪKSTOŠĀS GALERIJAS MODAS MIKROREZONATORA BĀZES VEIDOTA OPTISKO FREKVENČU ĶEMMES ĢENERATORA IZSTRĀDE UN TĀ PIELIETOJUMI TELEKOMUNIKĀCIJĀS