

# PERIODIC AND EVENTUALLY PERIODIC SOLUTIONS OF PIECEWISE LINEAR AND MAX-TYPE DIFFERENCE EQUATIONS

MICHAEL RADIN

*Rochester Institute of Technology School of Mathematical Sciences*

Rochester, New York 14623, U.S.A.

E-mail: michael.radin@rit.edu

We examine the existence of periodic solutions and eventually periodic solutions of Piecewise Linear and Max-Type Difference Equations; in particular we will start with the  $3X+1$  Conjecture, the Tent Map, the Collatz Equations and Max-Type Equations. In addition, we will investigate the uniqueness of the periodic orbits and the patterns of the periodic orbits as well. Furthermore, investigate which particular periods can exist under what circumstances. Moreover, discuss the boundedness of solutions and applications in neuron model(s).

## REFERENCES

- [1] William J. Briden, Edward A. Grove, Candace M. Kent, and Gerasimos Ladas, Eventually Periodic Solutions of  $x_{n+1} = \max \left\{ \frac{1}{x_n}, \frac{A_n}{x_{n-1}} \right\}$ , *Commun. Appl. Nonlinear Anal.* 6 (1999), no.4.
- [2] William J. Briden, Edward A. Grove, Gerasimos Ladas, and Lynn C. McGrath, On the Non-autonomous Equation  $x_{n+1} = \max \left\{ \frac{A_n}{x_n}, \frac{B_n}{x_{n-1}} \right\}$ , *Proceedings of the Third International Conference on Difference Equations and Applications*. September 1-5, 1997, Taipei, Taiwan, Gordon and Breach Science Publishers (1999), 49-73.
- [3] Edward A. Grove, Candace M. Kent, Gerasimos Ladas, and Michael A. Radin, On  $x_{n+1} = \max \left\{ \frac{1}{x_n}, \frac{A_n}{x_{n-1}} \right\}$  with a period 3 parameter. *Fields Institute Communications*. Volume 29, 2001, 161-180.
- [4] Candace M. Kent and Michael A. Radin, On the Boundedness Nature of the Positive Solutions of the Difference Equation  $x_{n+1} = \max \left\{ \frac{1}{x_n}, \frac{A_n}{x_{n-1}} \right\}$ , with Periodic Parameters. *Proceedings of the Third International DCDIS Conference on Engineering Applications and Computational Algorithms, Guelph, Ontario, Canada May 15, 2003*, Special Issue of the Dynamics of Discrete and Impulsive Systems, Series B: Applications and Algorithms, Watam Press, Waterloo. *Watam Press*. Volume 29, 2001, 11-15.