

J. Timoshenko, A. Kuzmin, J. Purans



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Abstract

Classical molecular dynamics (MD) simulations of the Ge K-edge EXAFS have been performed with the aim to estimate the thermal effects within the first three coordination shells and their influence on the single-scattering and multiple-scattering contributions. The effect of the isotopic mass has been also evaluated.

Introduction

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MD-EXAFS vs. Experiment

Experimental (T = 300 K) and configuration-averaged (T = 350 K, up to 6.5 Å) EXAFS spectra $\chi(k)k^2$ and

In this work we present for the first time the classical molecular dynamics (MD) simulation of the Ge K-edge EXAFS using recently developed approach [3].

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Interatomic forces: $F_i = -\nabla_i V(r_1, r_2, ..., r_n, \Theta_1, \Theta_2, ..., \Theta_m)$

Tersoff potential [4]:

$V(r_{1}, r_{2},, r_{n}, \Theta_{1}, \Theta_{2},, \Theta_{m}) = \sum_{i} V_{i} = \frac{1}{2} \sum_{i \neq j} V_{ij} \qquad b_{ij} = (1 + \beta^{n} \zeta_{ij}^{n})^{-1/2n} \\ V_{ij} = f_{C}(r_{ij}) [a_{ij} f_{R}(r_{ij}) + b_{ij} f_{A}(r_{ij})] \qquad \zeta_{ij} = \sum_{k \neq i, j} f_{C}(r_{ik}) g(\Theta_{ijk}) \exp[\lambda_{3}^{3}(r_{ij} - r_{jk})^{3}] \\ f_{A}(r) = -B \exp(-\lambda_{2} r) \\ f_{R}(r) = A \exp(-\lambda_{1} r) \qquad g(\Theta) = 1 + \frac{c^{2}}{d^{2}} - \frac{c^{2}}{d^{2} + (h - \cos\Theta)^{2}}$	A, keV B, keV λ ₁ , Å λ ₂ , Å	1.849 0.487 2.480 1.736	β · 10 ⁷ n λ ₃ , Å c · 10 ⁻⁵	4.357 0.436 1.732 1.015	Supe
$f_{C}(r) = \begin{cases} 1, & r < R - D \\ \frac{1}{2} - \frac{1}{2} \sin\left(\frac{\pi}{2} \frac{(r - R)}{D}\right), & R - D < r < R + D \\ 0, r > R + D \end{cases} a_{ij} = \left(1 + \alpha^{n} \eta_{ij}^{n}\right)^{-1/2n} \\ \eta_{ij} = \sum_{k \neq i,j} f_{C}(r_{ij}) \exp\left[\lambda_{3}^{3}(r_{ij} - r_{jk})^{3}\right] \end{cases}$	R D α	2.7 0.3 0	d h	17.51 -0.601	α_1
Stillinger-Weber (SW) potential [5]: $V(r_{1}, r_{2},, r_{n}, \Theta_{1}, \Theta_{2},, \Theta_{m}) = \frac{1}{2} \sum_{i,j} V_{ij} + \frac{1}{6} \sum_{i,j,k} V_{ijk} \qquad V_{ijk} = \varepsilon f_{3} \left(\frac{\vec{r}_{i}}{\sigma}, \frac{\vec{r}_{j}}{\sigma}, \frac{\vec{r}_{k}}{\sigma}\right)$	A B	7.050	λ V	31 1.2	c
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Force-field models: SW vs. Tersoff





MD-EXAFS: Temperature dependence of the multiple-scattering contribution



force-field 1)Stillinger-Weber (SW) The contribution from the

2nd and 3rd shells (peaks at ~ 3.7 and ~ 4.4 Å) are overestimated in the case of the Tersoff potential

The SW potential gives EXAFS signal being in better agreement with the experiment and will be used further.

Parallel MSRD (Debye-Waller factors)



Configuration-averaged EXAFS spectra $\chi(k)k^2$ (upper left panel) and their Fourier transforms (FTs) (lower left panel), calculated in the temperature range from 200 K to 450 K. Multiple-scattering contributions to EXAFS spectra (upper right panel) and their FTs (lower right panel).

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References

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